Why does preregistration increase the persuasiveness of evidence? A Bayesian

rationalization

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40 Abstract

The replication crisis has led many researchers to preregister their hypotheses and data 41 analysis plans before collecting data. A widely held view is that preregistration is supposed 42 to limit the extent to which data may influence the hypotheses to be tested. Only if data have no influence an analysis is considered confirmatory. Consequently, many researchers believe that preregistration is only applicable in confirmatory paradigms. In practice, researchers may struggle to preregister their hypotheses because of vague theories that necessitate data-dependent decisions (aka exploration). We argue that preregistration 47 benefits any study on the continuum between confirmatory and exploratory research. To that end, we formalize a general objective of preregistration and demonstrate that exploratory studies also benefit from preregistration. Drawing on Bayesian philosophy of science, we argue that preregistration should primarily aim to reduce uncertainty about the inferential procedure used to derive results. This approach provides a principled justification of preregistration, separating the procedure from the goal of ensuring strictly 53 confirmatory research. We acknowledge that knowing the extent to which a study is 54 exploratory is central, but certainty about the inferential procedure is a prerequisite for persuasive evidence. Finally, we discuss the implications of these insights for the practice of 56

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preregistration.

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The scientific community has long pondered the vital distinction between 63 exploration and confirmation, discovery and justification, hypothesis generation and hypothesis testing, or prediction and postdiction (Hoyningen-Huene, 2006; Nosek et al., 65 2018; Shmueli, 2010; Tukey, 1980). Despite the different names, it is fundamentally the same dichotomy that is at stake here. There is a broad consensus that both approaches are necessary for science to progress; exploration, to make new discoveries and confirmation, to expose these discoveries to potential falsification, and assess empirical support for the theory. However, mistaking exploratory findings for empirically confirmed results is dangerous. It inflates the likelihood of believing that there is evidence supporting a given hypothesis, even if it is false. A variety of problems, such as researchers' degrees of freedom together with researchers' hindsight bias or naive p-hacking have led to such mistakes becoming commonplace vet unnoticed for a long time. Recognizing them has led to a crisis of confidence in the empirical sciences (Ioannidis, 2005), and psychology in particular 75 (Open Science Collaboration, 2015). As a response to the crisis, evermore researchers preregister their hypotheses and their data collection and analysis plans in advance of their 77 studies (Nosek et al., 2018). They do so to stress the predictive nature of their registered 78 statistical analyses, often with the hopes of obtaining a label that marks the study as 79 "confirmatory". Indeed, rigorous application of preregistration prevents researchers from 80 reporting a set of results produced by an arduous process of trial and error as a simple 81 confirmatory story (Wagenmakers et al., 2012) while keeping low false-positive rates. This promise of a clear distinction between confirmation and exploration has obvious appeal to many who have already accepted the practice. Still, the majority of empirical researchers 84 do not routinely preregister their studies. One reason may be that some do not find that the theoretical advantages outweigh the practical hurdles, such as specifying every aspect of a theory and the corresponding analysis in advance. We believe that we can reach a greater acceptance of preregistration by explicating a more general objective of preregistration that
benefits all kinds of studies, even those that allow data-dependent decisions.

One goal of preregistration that has received widespread attention is to clearly
distinguish confirmatory from exploratory research (Bakker et al., 2020; Mellor & Nosek,
2018; Nosek et al., 2018; Simmons et al., 2021; Wagenmakers et al., 2012). In such a
narrative, preregistration is justified by a confirmatory research agenda. However, two
problems become apparent under closer inspection. First, many researchers do not
subscribe to a purely confirmatory research agenda (Baumeister, 2016; Brandmaier et al.,
2013; Finkel et al., 2017; Tukey, 1972). Second, there is no strict mapping of the categories
preregistered vs. non-preregistered onto the categories confirmatory vs. exploratory
research.

Obviously, researchers can conduct confirmatory research without preregistration—
though it might be difficult to convince other researchers of the confirmatory nature of
their research, that is, that they were free of cognitive biases, made no data-dependent
decisions, and so forth. The opposite, that is, preregistered but not strictly confirmatory
studies, are also becoming more commonplace (Chan et al., 2004; Dwan et al., 2008; Silagy
et al., 2002).

This is the result of researchers applying one of two strategies to evade the
self-imposed restrictions of preregistrations: writing a loose preregistration to begin with
(Stefan & Schönbrodt, 2023) or deviating from the preregistration afterward
(lakensWhenHowDeviate2024?). The latter is a frequent occurrence and, perhaps more
worryingly, often remains undisclosed (Akker et al., 2023; Claesen et al., 2021). Both
strategies may be used for sensible scientific reasons or with the self-serving intent of
generating desirable results. Thus, insisting on equating preregistration and confirmation
has led to the criticism that, all things considered, preregistration is actually harmful and
neither sufficient nor necessary for doing good science (Pham & Oh, 2021; Szollosi et al.,

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We argue that such criticism is not directed against preregistration itself but against 115 a justification through a confirmatory research agenda (Wagenmakers et al., 2012). When 116 researchers criticize preregistration as being too inflexible to fit their research question, they often simply acknowledge that their research goals are not strictly confirmatory. 118 Forcing researchers into adopting a strictly confirmatory research agenda does not only 119 imply changing how they investigate a phenomenon but also what research questions they 120 pose. However reasonable such a move is, changing the core beliefs of a large community is 121 much harder than convincing them that a method is well justified. We, therefore, attempt 122 to disentangle the methodological goals of preregistration from the ideological goals of 123 confirmatory science. It might well be the case that psychology needs more confirmatory 124 studies to progress as a science. However, independently of such a goal, preregistration can 125 be useful for any kind of study on the continuum between strictly confirmatory and fully 126 exploratory. 127

To form such an objective for preregistration, we first introduce some tools of Bayesian philosophy of science and map the exploration/confirmation distinction onto a dimensional quantity we call "theoretical risk" (a term borrowed from Meehl, 1978, but formalized as the probability of proving a hypothesis wrong if it does not hold).

We are interested in why preregistrations should change researchers' evaluation of
evidence. Applying a Bayesian framework allows us to investigate our research question
most straightforwardly because it directly deals with what we ought to believe, given the
evidence presented. Specifically, it allows us to model changes in subjective degrees of
belief due to preregistration or, more simply, "persuasion". Please note that our decision to
adopt a Bayesian philosophy of science does not make assumptions about the statistical
methods researchers use. In fact, this conceptualization is intentionally as minimal as
possible to be compatible with a wide range of philosophies of science and statistical

methods researchers might subscribe to. One feature of the Bayesian framework, is the 140 strong emphasis on subjective yet rational judgement. Therefore, we assume that 141 researchers will differ significantly in how they value evidence but that by making 142 assumptions about the general process, we can make general statements that apply to all 143 these subjective evaluations. However, we should note that Popperians would be appalled 144 that we are content with positive inductive inferences (but we regard "failing to disprove" 145 as too limited), and Neopopperians would flinch that we assign probabilities to beliefs (we 146 are fond of calculating things). While the latter move is not strictly necessary it allows us 147 to connect the more abstract considerations more closely with what researchers believe. 148

Now, we outline two possible perspectives on the utility of preregistration. The first 149 one corresponds to the traditional application of preregistration to research paradigms that 150 focus on confirmation by maximizing the theoretical risk or, equivalently, by limiting type-I 151 error (when dichotomous decisions about theories are an inferential goal). We argue that 152 this view on the utility of preregistration can be interpreted as maximizing theoretical risk, 153 which otherwise may be reduced by researchers' degrees of freedom, p-hacking, and suchlike. 154 The second interpretation is our main contribution: We argue that contrary to the classic 155 view, the objective of preregistration is not the maximization of theoretical risk but rather 156 the minimization of uncertainty about the theoretical risk. This interpretation leads to a 157 broad applicability of preregistration to both exploratory and confirmatory studies. 158

To arrive at this interpretation, we rely on three arguments. The first is that
theoretical risk is vital for judging evidential support for theories. The second argument is
that the theoretical risk for a given study is generally uncertain. The third and last
argument is that this uncertainty is reduced by applying preregistration. We conclude that
because preregistration decreases uncertainty about the theoretical risk, which in turn
increases the amount of knowledge we gain from a particular study, preregistration is
potentially useful for any kind of study, no matter where it falls on the

exploratory-confirmatory continuum.

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Persuation and the Bayesian rationale

If researchers plan to conduct a study, they usually hope that it will change their 168 assessment of some theory's verisimilitude (Niiniluoto, 1998). Moreover, they hope to 169 convince other researchers can be persuaded to change their believe in a theory as well. 170 Beforehand, researchers cannot know what evidence a study will provide but still must form 171 an expectation in order to decide about the specifics of a planned study, including if they 172 should preregister it. If they can expect that preregistration helps them to persuade other 173 researchers to change their believe, it is only rational to employ preregistration. To make 174 our three arguments, we must assume three things about what an ideal estimation process entails and how it relates to what studies (preregistered vs not preregistered) to conduct.

- 1. Researchers judge the evidence for or against a hypothesis rationally.
- 2. They expect other researchers to apply a similar rational process.
 - 3. Researchers try to maximize the expected persuasiveness for *other* researchers.

The assumption of rationality can be connected to Bayesian reasoning and leads to 180 our adoption of the framework. Our rationale is as follows. Researchers who decide to 181 conduct a certain study are actually choosing a study to bet on. They have to "place the 182 bet" by conducting the study by investing resources and stand to gain evidence for or 183 against a theory with some probability. This conceptualization of choosing a study as a 184 betting problem allows us to apply a "Dutch book" argument (Christensen, 1991). This 185 argument states that any better must follow the axioms of probability to avoid being 186 "irrational," i.e., accepting bets that lead to sure losses. Fully developing a Dutch book 187 argument for this problem requires careful consideration of what kind of studies to include 188 as possible bets, defining a conversion rate from the stakes to the reward, and modeling 189 what liberties researchers have in what studies to conduct. Without deliberating these 190 concepts further, we find it reasonable that researchers should not violate the axioms of 191

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probability if they have some expectation about what they stand to gain with some likelihood from conducting a study. The axioms of probability are sufficient to derive the Bayes formula, on which we will heavily rely for our further arguments. The argument is not sufficient, however, to warrant conceptualizing persuasiveness in terms of posterior probability; that remains a leap of faith. In fact, persuasiveness depends on how other researchers weigh evidence which differs between individuals.

However, the argument applies to any reward function that satisfies the "statistical relevancy condition" (Fetzer, 1974; Salmon, 1970), that is, evidence only increases believe for a theory if the evidence is more likely to be observed under the theory than under the alternative. In particular, "diagnosticity" (Fiedler, 2017; Oberauer & Lewandowsky, 2019), a concept highlighted in recent psychological literature, seems to adhere to the statistical relevancy condition.

Theoretical risk

Our first argument is that theoretical risk is crucial for judging the persuasiveness of evidence. Put simply, risky predictions create persuasive evidence if they turn out to be correct. This point is crucial because we attribute much of the appeal of a confirmatory research agenda to this notion.

Let us make some simplifying assumptions and define our notation. To keep the notation simple, we restrict ourselves to evidence of a binary nature (either it was observed or not). We denote the probability of a hypothesis before observing evidence as P(H) and its complement as $P(\neg H) = 1 - P(H)$. The probability of observing evidence under some hypothesis is P(E|H). We can calculate the probability of the hypothesis after observing the evidence with the help of the Bayes formula:

$$P(H|E) = \frac{P(H)P(E|H)}{P(E)} \tag{1}$$

The posterior probability P(H|E) is of great relevance since it is often used directly 215 or indirectly as a measure of confirmation of a hypothesis. In the tradition of Carnap, in its 216 direct use, it is called *confirmation as firmness*; in its relation to the a priori probability 217 P(H), it is called *increase in firmness* (Carnap, 1950, preface to the 1962 edition). We 218 concentrate on the posterior probability because of its simplicity but take it only as one 219 example of a possible measure. In reality, researchers surely differ in what function they 220 apply to judge evidence and it is often most fruitful to compare more than two competing 221 hypotheses. The goal is therefore to reason about the space of possible measures 222 researchers might apply. However, since any measure fulfilling the statistical relevancy 223 condition increases monotonically with an increase in posterior probability P(H|E), we 224 might well take it to illustrate our reasoning. 225

In short, we want to increase posterior probability P(H|E). Increases in posterior 226 probability P(H|E) are associated with increases in persuasiveness, of which we want to 227 maximize the expectation. So how can we increase posterior probability? The Bayes 228 formula yields three components that influence confirmation, namely P(H), P(E|H) and 229 P(E). The first option leads us to the unsurprising conclusion that higher a priori 230 probability P(H) leads to higher posterior probability P(H|E). If a hypothesis is more 231 probable to begin with, observing evidence in its favor will result in a hypothesis that is 232 more strongly confirmed, all else being equal. However, the prior probability of a 233 hypothesis is nothing our study design can change. The second option is equally 234 reasonable; that is, an increase in P(E|H) leads to a higher posterior probability P(H|E). 235 P(E|H) is the probability of obtaining evidence for a hypothesis when it holds. We call this probability of detecting evidence, given that the hypothesis holds "detectability." 237 Consequently, researchers should ensure that their study design allows them to find 238 evidence for their hypothesis, in case it is true. When applied strictly within the bounds of 239 null hypothesis testing, detectability is equivalent to power (or the complement of type-II 240 error rate). However, while detectability is of great importance for study design, it is not 241

directly relevant to what a preregistration is communicating to other researchers. We later
discuss how issues of detectability must be considered in a preregistration. Thus, P(E)remains to be considered. Since P(E) is the denominator, decreasing it can increase the
posterior probability. In other words, high risk, high reward.

If we equate riskiness with a low probability of obtaining evidence (when the 246 hypothesis is false), the Bayesian rationale perfectly aligns with the observation that risky 247 predictions lead to persuasive evidence. This tension between high risk leading to high gain 248 is central to our consideration of preregistration. A high-risk, high-gain strategy is bound 249 to result in many losses that are eventually absorbed by the high gains. Sustaining many 250 "failed" studies is not exactly aligned with the incentive structure under which many, if not 251 most, researchers operate. Consequently, researchers are incentivized to appear to take 252 more risks than they actually do, which misleads their readers to give their claims more 253 credence than they deserve. It is at this juncture that the practice and mispractice of 254 preregistration comes into play. We argue that the main function of preregistration is to 255 enable proper judgment of the riskiness of a study. 256

To better understand how preregistrations can achieve that, let us take a closer look at the factors contributing to P(E). Using the law of total probability, we can split P(E)into two terms:

$$P(E) = P(H)P(E|H) + P(\neg H)P(E|\neg H)$$
(2)

We have already noted that there is not much to be done about prior probability $(P(H), \text{ and hence its counter probability } P(\neg H))$, and that it is common sense to increase detectability P(E|H). The real lever to pull is therefore $P(E|\neg H)$. This probability tells us how likely it is that we find evidence in favor of the theory when in fact, the theory is not true. Its counter probability $P(\neg E|\neg H) = 1 - P(E|\neg H)$ is what we call "theoretical

risk", because it is the risk a theory takes on in predicting the occurrence of particular evidence in its favor. We borrow the term from Meehl (1978), though he has not assigned it to the probability $P(\neg E|\neg H)$. Kukla (1990) argued that the core arguments in Meehl (1990) can be reconstructed in a purely Bayesian framework. However, while he did not mention $P(\neg E|\neg H)$ he suggested that Meehl (1978) used the term "very strange coincidence" for a small $P(E|\neg H)$ which would imply, that $P(\neg E|\neg H)$ can be related to or even equated to theoretical risk.

Let us note some interesting properties of theoretical risk $P(\neg E|\neg H)$. First, 272 increasing theoretical risk leads to higher posterior probability P(H|E), our objective. 273 Second, if the theoretical risk is smaller than detectability P(E|H) it follows that the 274 posterior probability must decrease when observing the evidence. If detectability exceeds 275 theoretical risk, the evidence is less likely under the theory than it is when the theory does 276 not hold (the inverse of statistical relevancy). Third, if the theoretical risk equals zero, then 277 posterior probability is at best equal to prior probability but only if detectability is perfect 278 P(H|E) = 1). In other words, observing a sure fact does not lend credence to a hypothesis. 279

The last statement sounds like a truism but is directly related to Popper's seminal criterion of demarcation. He stated that if it is impossible to prove that a hypothesis is false $(P(\neg E|\neg H) = 0$, theoretical risk is zero), it cannot be considered a scientific hypothesis (Popper, 2002, p. 18). We note these relations to underline that the Bayesian rationale we apply here is able to reconstruct many commonly held views on how "risky" predictions are valued (but we of course differ from Popper on the central role of induction in science).

Both theoretical risk $P(\neg E|\neg H)$ and detectability P(E|H) aggregate countless influences; otherwise, they could not model the process of evidential support for theories. To illustrate the concepts we have introduced here, consider the following example of a single theory and three experiments that may test it. The experiments were created to illustrate how they may differ in their theoretical risk and detectability. Suppose the

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primary theory is about the cognitive phenomenon of "insight." For the purpose of illustration, we define it, with quite some hand-waving, as a cognitive abstraction that allows agents to consistently solve a well-defined class of problems. We present the hypothesis that the following problem belongs to such a class of insight problems:

Use five matches (IIIII) to form the number eight.

We propose three experiments that differ in theoretical risk and detectability. All
experiments take a sample of ten psychology students. We present the students with the
problem for a brief span of time. After that, the three experiments differ as follows:

- 1. The experimenter gives a hint that the problem is easy to solve when using Roman numerals; if all students come up with the solution, she records it as evidence for the hypothesis.
- 2. The experimenter shows the solution "VIII" and explains it; if all students come up with the solution, she records it as evidence for the hypothesis.
- 30. The experimenter does nothing; if all students come up with the solution, she records
 it as evidence for the hypothesis.

We argue that experiment 1 has high theoretical risk $P(\neg E_1|\neg H)$ and high 306 detectability $P(E_1|H)$. If "insight" has nothing to do with solving the problem $(\neg H)$, then 307 presenting the insight that Roman numerals can be used should not lead to all students 308 solving the problem $(\neg E_1)$; the experiment, therefore, has high theoretical risk 309 $P(\neg E_1|\neg H)$. Conversely, if insight is required to solve the problem (H), then it is likely to 310 help all students to solve the problem (E_1) , the experiment, therefore, has high 311 detectability $P(E_1|H)$. The second experiment, on the other hand, has low theoretical risk 312 $P(\neg E_2|\neg H)$. Even if "insight" has nothing to do with solving the problem $(\neg H)$, there are 313 other plausible reasons for observing the evidence (E_2) , because the students could simply 314 copy the solution without having any insight. With regard to detectability, experiments 1 315

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and 2 differ in no obvious way. Experiment 3, however, also has low detectability. It is 316 unlikely that all students will come up with the correct solution in a short time (E_3) , even 317 if insight is required (H); experiment 3 therefore has low detectability $P(E_3|H)$. The 318 theoretical risk, however, is also low in absolute terms, but high compared to the 319 detectability (statistical relevancy condition is satisfied). In the unlikely event that all 10 320 students place their matches to form the Roman numeral VIII (E_3) , it is probably due to 321 insight (H) and not by chance $P(\neg E_3|\neg H)$). Of course, in practice, we would allow the 322 evidence to be probabilistic, e.g., relax the requirement of "all students" to nine out of ten 323 students, more than eight, and so forth. 324

As mentioned earlier, the we restrict ourselves to binary evidence, to keep the mathematical notation as simple as possible. We discuss the relation between statistical methods and theoretical risk in the Statistical Methods section.

Preregistration as a means to increase theoretical risk?

Having discussed that increasing the theoretical risk will increase the persuasiveness, it is intuitive to task preregistration with maximizing theoretical risk, i.e., a confirmatory research agenda. Indeed, limiting the type-I error rate is commonly stated as *the* central goal of preregistration (Nosek et al., 2018; Oberauer, 2019; Rubin, 2020). We argue that while such a conclusion is plausible, we must first consider at least two constraints that place an upper bound on the theoretical risk.

First, the theory itself limits theoretical risk: Some theories simply do not make
risky predictions, and preregistration will not change that. Consider the case of a
researcher contemplating the relation between two sets of variables. Suppose each set is
separately well studied, and strong theories tell the researcher how the variables within the
set relate. However, our imaginary researcher now considers the relation between these two
sets. For lack of a better theory, they assume that some relation between any variables of
the two sets exists. This is not a risky prediction to make in psychology (Orben & Lakens,

from this rather exploratory study to develop a more precise (and therefore risky) theory,
e.g., by using the results to specify which variables from one set relate to which variables
from the other set, to what extent, in which direction, with which functional shape, etc., to
be able to make riskier predictions in the future. We will later show that preregistration
increases the degree of belief in the further specified theory, though it remains low till
being substantiated by testing the theory again. This is because preregistration increases
the expected persuasiveness regardless of the theory being tested, as we will show.

Second, available resources limit theoretical risk. Increasing theoretical risk 350 $P(\neg E|\neg H)$ will usually decrease detectability P(E|H) unless more resources are invested. 351 This is similar to the well known tradeoff between type-I error rate and statistical power. 352 Tasking preregistration with an increase in theoretical risk makes it difficult to balance this 353 trade-off. Mindlessly maximizing theoretical risk would either never produce evidence or 354 require huge amounts of resources. As noted before, we strive for high detectability and 355 high theoretical risk in planning, conducting, and analyzing studies. Maximizing one at the 356 expense of the other is not necessarily beneficial for increasing persuasiveness but depends 357 on the specific function they apply to judge evidence and their specific location on the 358 curve. One advantage of our framework is that researchers can employ it to balance the 359 trade-off more effectively assuming they are willing to make some simplifying assumptions. 360

Uncertainty about theoretical risk

We have established that higher theoretical risk leads to more persuasive evidence.

In other words, we have reconstructed the interpretation that preregistrations supposedly
work by restricting the researchers, which in turn increases the theoretical risk (or
equivalently limits the type-I error rate) and thereby creates more compelling evidence.

Nevertheless, there are trade-offs for increasing theoretical risk. Employing a mathematical
framework allows us to navigate the trade-offs more effectively and move towards a second,

more favorable interpretation. To that end, we incorporate uncertainty about theoretical risk into our framework.

370 Statistical methods

One widely known factor is the contribution of statistical methods to theoretical 371 risk. Theoretical risk $P(\neg E|\neg H)$ is deeply connected with statistical methods, because it is 372 related to the type-I error rate in statistical hypothesis testing $P(E|\neg H)$ by $P(\neg E|\neg H)=1-P(E|\neg H),$ if you consider the overly simplistic case where the research 374 hypothesis is equal to the statistical alternative-hypothesis because then the nill-hypothesis 375 is $\neg H$. Because many researchers are familiar with the type-I error rate, it can be helpful 376 to remember this connection to theoretical risk. Researchers who choose a smaller type-I 377 error rate can be more sure of their results, if significant, because the theoretical risk is 378 higher. However, this connection should not be overinterpreted for two reasons. First, 379 according to most interpretations of null hypothesis testing, the absence of a significant 380 result should not generally be interpreted as evidence against the hypothesis (Mayo, 2018, 381 p. 5.3). Second, the research hypothesis rarely equals the statistical alternative hypothesis 382 (most research hypothesis are more specific than "any value except zero"). In fact, it is 383 entirely possible to assume the null hypothesis as a research hypothesis, as is commonly 384 done in e.g., structural equation modelling, where the roles of detectability, theoretical risk 385 and type-I/II error rate switch. We argue that theoretical risk (and hence its complement, 386 $P(E|\neg H)$) also encompasses factors outside the statistical realm, most notably the study 387 design and broader analytical strategies. Type-I error rate is the property of a statistical 388 test under some assumptions, whereas theoretical risk is a researchers' belief. One may 389 take such theoretical properties as a first starting point to form a substantive belief but 390 surely researchers ought to take other factors into consideration. For example, if a 391 researcher believes that there might be confounding variables at play for the relation 392 between two variables, this should decrease theoretical risk; after all they might find an 393 association purely on account of the confounders (Fiedler, 2017).

Statistical methods stand out among these factors because we have a large and well-understood toolbox for assessing and controlling their contribution to theoretical risk. Examples of our ability to exert this control are the choice of type-I error rate, adjustments for multiple testing, the use of corrected fit measures (i.e., adjusted R^2), information criteria, or cross-validation in machine learning. These tools help us account for biases in statistical methods that influence theoretical risk (and hence, $P(E|\neg H)$).

The point is that the contribution of statistical methods to theoretical risk can be 401 formally assessed. For many statistical models it can be analytically computed under some 402 assumptions. For those models or assumptions where this is impossible, one can employ 403 Monte Carlo simulation to estimate the contribution to theoretical risk. The precision with 404 which statisticians can discuss contributions to theoretical risk has lured the community 405 concerned with research methods into ignoring other factors that are much more uncertain. 406 We cannot hope to resolve this uncertainty; but we have to be aware of its implications. 407 These are presented in the following. 408

409 Sources of uncertainty

As we have noted, it is possible to quantify how statistical models affect the 410 theoretical risk based on mathematical considerations and simulation. However, other 411 factors in the broader context of a study are much harder to quantify. If one chooses to 412 focus only on the contribution of statistical methods to theoretical risk, one is bound to 413 overestimate it. Take, for example, a t-test of mean differences in two samples. Under ideal 414 circumstances (assumption of independence, normality of residuals, equal variance), it 415 stays true to its type-I error rate. However, researchers may do many very reasonable 416 things in the broader context of the study that affect theoretical risk: They might exclude 417 outliers, choose to drop an item before computing a sum score, broaden their definition of 418 the population to be sampled, translate their questionnaires into a different language, 419 impute missing values, switch between different estimators of the pooled variance, or any

number of other things. All of these decisions carry a small risk that they will increase the 421 likelihood of obtaining evidence despite the underlying research hypothesis being false. 422 Even if the t-test itself perfectly maintains its type I error rate, these factors influence 423 $P(E|\neg H)$. While, in theory, these factors may leave $P(E|\neg H)$ unaffected or even decrease 424 it, we argue that this is not the case in practice. Whether researchers want to or not, they 425 continuously process information about how the study is going, except under strict 426 blinding. While one can hope that processing this information does not affect their 427 decision-making either way, this cannot be ascertained. Therefore, we conclude that 428 statistical properties only guarantee a lower bound for theoretical risk. The only thing we 429 can conclude with some certainty is that theoretical risk is not higher than what the 430 statistical model guarantees without knowledge about the other factors at play. 431

The effects of uncertainty

Before we ask how preregistration influences this uncertainty, we must consider the 433 implications of being uncertain about the theoretical risk. Within the Bayesian framework, 434 this is both straightforward and insightful. Let us assume a researcher is reading a study 435 from another lab and tries to decide whether and how much the presented results confirm 436 the hypothesis. As the researcher did not conduct the study (and the study is not 437 preregistered), they can not be certain about the various factors influencing theoretical risk 438 (researcher degrees of freedom). We therefore express this uncertainty about the theoretical 439 risk as a probability distribution Q of $P(E|\neg H)$ (remember that $P(E|\neg H)$ is related to 440 theoretical risk by $P(E|\neg H) = 1 - P(\neg E|\neg H)$, so it does not matter whether we consider 441 the distribution of theoretical risk or $P(E|\neg H)$). To get the expected value of P(H|E)442 that follows from the researchers' uncertainty about the theoretical risk, we can compute 443 the expectation using Bayes theorem:

$$\mathbb{E}_{Q}[P(H|E)] = \mathbb{E}_{Q}\left[\frac{P(H)P(E|H)}{P(H)P(E|H) + P(\neg H)P(E|\neg H)}\right] \tag{3}$$

Of course, the assigned probabilities and the distribution Q vary from study to 445 study and researcher to researcher (and even the measure of confirmation), but we can 446 illustrate the effect of uncertainty with an example. Assuming P(E|H) = 0.8 (relective of 447 the typically strived for power of 80%). Let us further assume that the tested hypothesis is 448 considered unlikely to be true by the research community before the study is conducted 449 (P(H) = 0.1) and assign a uniform distribution for $P(E|\neg H) \sim U([1-\tau,1])$ where τ is set 450 to $1-\alpha$, reflecting our assumption that this term gives an upper bound for theoretical risk 451 $P(\neg E|\neg H)$. We chose this uniform distribution as it is the maximum entropy distribution 452 with support $[1-\tau,1]$ and hence conforms to our Bayesian framework (Giffin & Caticha, 453 2007).

With this, we derive the expected value of P(H|E) as

$$\mathbb{E}_{Q}[P(H|E)] = \mathbb{E}_{Q}\left[\frac{P(H)P(E|H)}{P(H)P(E|H) + P(\neg H)P(E|\neg H)}\right] \tag{4}$$

$$= \int_{[1-\tau,1]} \tau^{-1} \frac{P(H)P(E|H)}{P(H)P(E|H) + P(\neg H)P(E|\neg H)} dP(E|\neg H)$$
 (5)

$$=\frac{P(H)P(E|H)}{P(\neg H)\tau}\ln\left(\frac{P(H)P(E|H)+P(\neg H)}{P(H)P(E|H)+P(\neg H)(1-\tau)}\right) \tag{6}$$

Figure 1 shows exemplary the effect of theoretical risk (x-axis) on the posterior
probability (y-axis) being certain (solid line) or uncertain (dashed line) about the
theoretical risk of a study. Our expectation of the persuasiveness varies considerably
depending on how uncertain we are about the theoretical risk a study took on.

Mathematically, uncertainty about theoretical risk is expressed through the variance (or
rather entropy) of the distribution. The increase in uncertainty (expressed as more entropic
distributions) leads to a decreased expected persuasiveness.

The argument for a confirmatory research agenda is that by increasing theoretical risk we increase expected persuasiveness, i.e., moving to the right on the x-axis in Figure 1

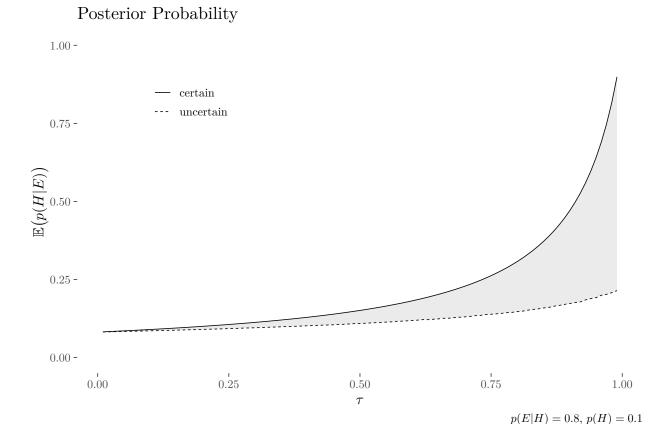


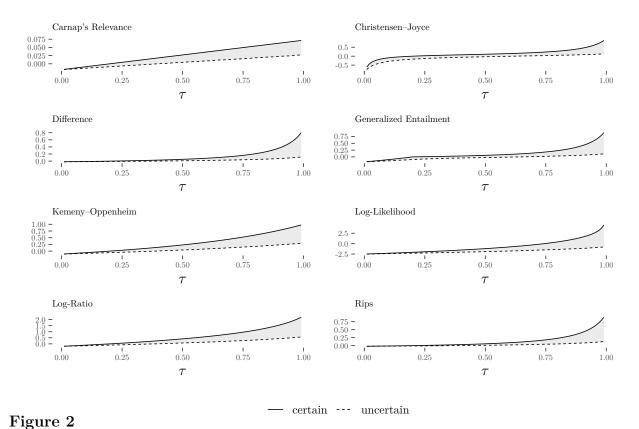
Figure 1

Posterior probability (confirmation as firmness) as a function of theoretical risk τ , where τ is either certain (solid line) or maximally uncertain (dotted line).

increases posterior probability (on the y-axis). However, if a hypothesis in a certain study 464 has low theoretical risk, there is not much researchers can do about it. However, studies do 465 not only differ by how high the theoretical risk is but also by how certain the recipient is 466 about the theoretical risk. A study that has a very high theoretical risk (e.g., 1.00% chance 467 that if the hypothesis is wrong, evidence in its favor will be observed,) but has also 468 maximum uncertainty will result in a posterior probability of 21%, while the same study 469 with maximum certainty will result in 90% posterior probability. The other factors 470 (detectability, prior beliefs, measure of confirmation) and, therefore, the extent of the 471 benefit varies, of course, with the specifics of the study. Crucially, even studies with some 472 exploratory aspects benefit from preregistration, e.g., in this scenario with a $\tau = 0.80$ (false 473

Sprenger and Hartmann (2019), Table 1.3, p. 51.

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Several measures for confirmation as an increase in firmness as a function of τ , where τ is either certain (solid line) or maximally uncertain (dotted line). Measures taken from

positive rate of 0.20) moving from uncertain to certain increases the posterior from 0.15 to 0.31. We find it helpful to calculate an example because of the nonlinear nature of the evidence functions.

Preregistration as a means to decrease uncertainty about the theoretical risk

We hope to have persuaded the reader to accept two arguments: First, the
theoretical risk is important for judging evidential support for theories. Second, the
theoretical risk is inherently uncertain, and the degree of uncertainty diminishes the
persuasiveness of the gathered evidence. The third and last argument is that
preregistrations reduce this uncertainty. Following the last argument, a preregistered study
is represented by the solid line (certainty about theoretical risk), and a study that was not

preregistered is more similar to the dashed line (maximally uncertain about theoretical risk) in Figure 1 and Figure 2.

Let us recall our three assumptions:

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- 1. Researchers judge the evidence for or against a hypothesis rationally.
- 2. They expect other researchers to apply a similar rational process.
 - 3. Researchers try to maximize the expected persuasiveness for other researchers.

The point we make with these assumptions is that researchers aim to persuade 490 other researchers, for example, the readers of their articles. Not only the original authors 491 are concerned with the process of weighing evidence for or against a theory but really the 492 whole scientific community the study authors hope to persuade. Unfortunately, readers of a 493 scientific article (or, more generally, any consumer of a research product) will likely lack 494 insight into the various factors that influence theoretical risk. While the authors 495 themselves may have a clear picture of what they did and how it might have influenced the 496 theoretical risk they took, their readers have much greater uncertainty about these factors. 497 In particular, they never know which relevant factors the authors of a given article failed to 498 disclose, be it intentionally or not. From the perspective of the ultimate skeptic, they may 490 claim maximum uncertainty. 500

Communicating clearly how authors of a scientific report collected their data and 501 consequently analyzed it to arrive at the evidence they present is crucial for judging the 502 theoretical risk they took. Preregistrations are ideal for communicating just that because 503 any description after the fact is prone to be incomplete. For instance, the authors could 504 have opted for selective reporting, that is, they decided to exclude a number of analytic 505 strategies they tried out. That is not to say that every study that was not-preregistered 506 was subjected to practices of questionable research practices. The point is that we cannot 507 exclude it with certainty. This uncertainty is drastically reduced if the researchers have 508

described what they intended to do beforehand and then report that they did exactly that.

In that case, readers can be certain they received a complete account of the situation.

They still might be uncertain about the actual theoretical risk the authors took, but to a

much smaller extent than if the study would not have been preregistered.

The remaining sources of uncertainty might be unfamiliarity with statistical methods or experimental paradigms used, the probability of an implementation error in the statistical analyses, a bug in the software used for analyses, etc. To further reduce the uncertainty about theoretical risk, researchers must therefore publish code and ideally data. After all, computational reproducibility is only possible if the data analytic procedure was communicated clearly enough to allow others to retrace the computational steps (Peikert & Brandmaier, 2021).

In any case, a well-written preregistration should aim to reduce the uncertainty about the theoretical risk and hence increase the persuasiveness of evidence. Therefore, a study that perfectly adhered to its preregistration will resemble the solid line in Figure 1/2. Crucially, perfect means here that the theoretical risk can be judged with low uncertainty, not that the theoretical risk is necessarily high.

Hacking, harking, and other harms

The importance of distinguishing between low and highly uncertain theoretical risk becomes perhaps clearer if we consider a few hypothetical cases for illustration.

- 1. We know with absolute certainty that researchers will revert to p-hacking to create evidence that is favorable for the theory.
- 2. A hypothesis was picked to explain reported results after the fact (HARKing, Kerr, 1998).
 - 3. We cannot exclude the possibility of p-hacking having led to the reported results.
 - 4. Reported results were obtained by planned exploration.

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5. Reported results were obtained by unplanned exploration.

In case 1, there is no theoretical risk $(P(\neg E|\neg H) = 0)$. If we know that the results 535 will be engineered to support the hypothesis no matter what, there is no reason to collect data. A prime example of this case is the $p_{\text{pointless}}$ metric (Hussey, 2021). Case 2 has a 537 similar problem. After all, the hypothesis that it had to happen the way it did happen is 538 irrefutable. In fact, both cases should be problematic to anyone who subscribes to the 539 statistical relevancy condition because if we choose the hypothesis in accordance with the 540 data or vice versa, without restrictions, they are not related anymore (i.e., observing the 541 data does not tell us anything about the hypothesis and the other way around). Case 3 is 542 different since here the theoretical risk is not necessarily low but simply uncertain (and 543 perhaps best represented by the dotted line in Figure 1/2). In case 4, the theoretical risk is 544 neither zero (unless the researcher plans to do run variations of analyses until a favourable 545 outcome is obtained, then we have a particular instance case of 1) nor high (as this is the 546 nature of exploratory approaches). However, we can take advantage of computational 547 reproducibility, use statistical properties, simulation or resampling methods, together with 548 scientific reasoning, to get a reasonably certain evaluation of the theoretical risk and hence 549 are in a somewhat favourable position (i.e., close to the solid line in n Figure 1/2). This 550 favorable position leads us to recommend preregistration of exploratory studies. Case 5 551 shares the neither zero nor high theoretical risk of case 4 but has additional uncertainty 552 about how much exploration was going on (how hard did researcher try to come up with favourable results). Its low and uncertain theoretical risk make it difficult to produce compelling evidence. 555

556 Discussion

To summarize, we showed that both higher theoretical risk and lower uncertainty about theoretical risk lead to higher persuasiveness across a variety of measures. The former result that increasing theoretical risk leads to higher expected persuasiveness

reconstructs the appeal and central goal of preregistration of confirmatory research 560 agendas. However, theoretical risk is something researchers have only limited control over. 561 For example, theories are often vague and ill-defined, resources are limited, and increasing 562 theoretical risk usually decreases detectability of a hypothesized effect (a special instance of 563 this trade-off is the well-known tension between type-I error and statistical power). While 564 we believe that preregistration is always beneficial, it might be counterproductive to pursue 565 high theoretical risk if the research context is inappropriate for strictly confirmatory 566 research. Specifically, appropriateness here entails the development of precise theories and 567 the availability of necessary resources (often, large enough sample size, but also see 568 Brandmaier et al. (2015)) to adequately balance detectability against theoretical risk. 569

In terms of preparing the conditions for confirmatory research, preregistration may 570 at most help to invest some time into developing more specific, hence riskier, implications 571 of a theory. But for a confirmatory science, it will not be enough to preregister all studies. 572 This undertaking requires action from the whole research community (Lishner, 2015). 573 Incentive structures must be created to evaluate not the outcomes of a study but the rigor 574 with which it was conducted (Cagan, 2013; Schönbrodt et al., 2022). Journal editors could 575 encourage theoretical developments that allow for precise predictions that will be tested by 576 other researchers and be willing to accept registered reports (Fried, 2020a, 2020b; van 577 Rooij & Baggio, 2021, 2020). Funding agencies should demand an explicit statement about 578 theoretical risk in relation to detectability and must be willing to provide the necessary 579 resources to reach adequate levels of both (Koole & Lakens, 2012).

Theoretical risk may conceptually be related to the framework of "severity" (Mayo, 2018; Mayo & Spanos, 2011). However, there are crucial differences between the two. First, our perspective on theoretical risk is not primarily concerned with avoiding inductive reasoning but with subjective changes of belief. This is important because, while severity is calculable, it remains unclear how severity should be valued, e.g. if an increase in severity

from .80 to .81 should be as impressive as from .99 to .999. Second, severity considerations
are mainly after the fact. Severity, a measure with which we can rule out alternative
explanations, can only be calculated after evidence was observed. However, there also are
communalities, like the strong emphasis on counterfactual consideration (imagining the
hypothesis was false), and there are even proposals to reconcile Bayesian and severity
considerations (van Dongen et al., 2023).

Our latter result, on the importance of preregistration for minimizing uncertainty, 592 has two important implications. The first is, that even if all imaginable actions regarding 593 promoting higher theoretical risk are taken, confirmatory research should be preregistered. 594 Otherwise, the uncertainty about the theoretical risk will diminish the advantage of 595 confirmatory research. Second, even under less-than-ideal circumstances for confirmatory 596 research, preregistration is beneficial. Preregistering exploratory studies increases the 597 expected persuasiveness by virtue of reducing uncertainty about theoretical risk. 598 Nevertheless, exploratory studies will have a lower expected persuasiveness than a more 590 confirmatory study if both are preregistered and have equal detectability. 600

Focusing on uncertainty reduction also explains two common practices of 601 preregistration that do not align with a confirmatory research agenda. First, researchers 602 seldomly predict precise numerical outcomes, instead they use preregistrations to describe 603 the process that generates the results. Precise predictions would have very high theoretical 604 risk (they are likely incorrect if the theory is wrong). A statistical procedure may have high 605 or low theoretical risk depending on the specifics of the model used. Specifying the process, 606 therefore, is in line with the rationale we propose here, but is less reasonable when the goal 607 of preregistration is supposed to be a strictly confirmatory research agenda. 608

Second, researchers often have to deviate from the preregistration and make
data-dependent decisions after the preregistration. If the only goal of preregistration is to
ensure confirmatory research, such changes are not justifiable. However, under our rational,

some changes may be justified. Any change increases the uncertainty about the theoretical 612 risk and may even decrease the theoretical risk. The changes still may be worthwhile if the 613 negative outcomes may be offset by an increase in detectability due to the change. 614 Consider a preregistration that failed to specify how to handle missing values, and 615 researchers subsequently encountering missing values. In such case, detectability becomes 616 zero because the data cannot be analyzed without a post-hoc decision about how to handle 617 the missing data. Any such decision would constitute a deviation from the preregistration, 618 which is possible under our proposed objective. Note that a reader cannot rule out that the 619 researchers leveraged the decision to decrease theoretical risk, i.e., picking among all 620 options the one that delivers the most beneficial results for the theory (in the previous 621 example, chosing between various options of handling missing values). Whatever decision 622 they make, increased uncertainty about the theoretical risk is inevitable and the expected persuasiveness is decreased compared to a world where they anticipated the need to deal with missing data. However, it is still justified to deviate. After all they have not anticipated the case and are left with a detectability of zero. Any decision will increase 626 detectability to a non-zero value offsetting the increase in uncertainty. The researchers also 627 may do their best to argue that the deviation was not motivated by increasing theoretical risk, thereby, decreasing the uncertainty. Ideally, there is a default decision that fits well 629 with the theory or with the study design. Or, if there is no obvious candidate, the 630 researchers could conduct a multiverse analysis of the available options to deal with 631 missings to show the influence of the decision (Steegen et al., 2016). In any case, deviations 632 must be transparently reported and we applaud recent developments to standardize and 633 normalize this process (Willroth & Atherton, 2023). 634

As explained above, reduction in uncertainty as the objective for preregistration does not only explain some existing practice, that does not align with confirmation as a goal, it also allows to form recommendations to improve the practice of preregistration.

Importantly, we now have a theoretical measure to gauge the functionality of

preregistrations, which can only help increase its utility. In particular, a preregistration
should be specific about the procedure that is intended to generate evidence for a theory.

Such a procedure may accommodate a wide range of possible data, i.e., it may be
exploratory. The theoretical risk, however low, must be communicated clearly. Parts of the
process left unspecified imply uncertainty, which preregistration should reduce. However,
specifying procedures that can be expected to fail will lead to deviation and, subsequently,
to larger uncertainty.

Our emphasis on transparency aligns with other justifications of preregistration, 646 especially those put forth by Lakens (2019)'s, although based on quite different 647 philosophical foundations. Our goal is to contribute a rationale that more comprehensively 648 captures the spectrum of exploration and confirmation in relation to preregistrations, 649 post-hoc changes of preregistrations, and subjective evaluations of evidence. We find it 650 difficult to content ourselves with vague terms like "control" or "transparency" if they 651 ultimately remain unconnected to how much researchers believe in a theory. Within our 652 framework, researchers have the ability to input their assumptions regarding the 653 perspectives of other researchers and calculate the potential impact of their actions on their 654 readership, whether these actions relate to study design, to the preregistration itself, or 655 subsequent deviations from it. We put subjective evaluations at the center of our 656 considerations; we deal explicitly with researchers who are proponents of some theory (they 657 have higher priors for the theory being true), researchers who suspect confounding variables (they assume lower theoretical risk), or those who remain doubtful if everything relevant 659 was reported (they have higher uncertainty about theoretical risk) or even those who place greater value on incongruent evidence than others (they differ in their confirmation 661 function). We, therefore, hope to not only provide a rationale for preregistration for those 662 who subscribe to a Bayesian philosophy of science but also a framework to navigate the 663 complicated questions that arise in the practice of preregistration.

At the same time, approaching the evaluation of evidence using a Bayesian 665 formalism is far from novel Fiedler (2017). To our knowledge, it was not yet applied to the 666 problem of preregistration. However, Oberauer and Lewandowsky (2019) made use of the 667 formalism to model the relation between theory, hypothesis, and evidence. In the context 668 of this conceptualization, they discussed the usefulness of preregistration, though without 669 applying the formalism there. Most importantly, they are rather critical of the idea that 670 preregistration has tangible benefits. Instead, they prefer multiverse analyses but contend 671 that those could be preregistered if one fancies it. Their reasoning is based on two 672 intuitions about what should not influence the evaluation of evidence: temporal order and 673 the mental state of the originator. In our opinion, they disregard the temporal order a bit 674 too hastily, as it is a long-standing issue in Bayesian philosophy of science known as the 675 "problem of old evidence" (Chihara, 1987). However, we agree that not the temporal order is decisive but if the researchers incorporated the information into the hypothesis the 677 evidence is supposed to confirm. For the other, we argue that the mental state of the 678 originator does matter. Suppose there are k = 1, 2, ..., K ways to analyze data, where each 679 k has a $P(E_k|\neg H)>0$. If they intend to try each way after another but happen to be 680 "lucky" on the first try and stop, should we then apply $P(E|\neg H) = P(E_1|\neg H)$ or 681 $P(E|\neg H) = P(E_1 \lor \dots \lor E_k|\neg H)$? We think the latter. However, this "Defeatist" intuition 682 is not universally warranted and depends on what we take H to mean specifically (Kotzen, 683 2013). Addressing, this problem might benefit from combining Oberauer and Lewandowsky 684 (2019)'s idea of updating on two nested levels (theory-hypothesis layered on top of 685 hypothesis-evidence) with our approach to modelling uncertainty. 686

Whatever the difference in evaluating preregistration as a tool, maybe conceptually more profound is that Oberauer and Lewandowsky (2019) conceptualizes "discovery-oriented research" differently than we do "exploratory". They assume the same theoretical risk $(P(\neg E|\neg H) = .05)$ and detectability (P(E|H)) = .8) in their calculation example as we do but assign different prior probabilities, namely .06 for discovery versus .6

for theory testing. Then, they conclude that discovery-oriented researcher requires a much 692 lower type-I error rate to control false positive in light of the low prior probability. This 693 runs counter to our definition of exploratory research having low theoretical risk. Of course, 694 we agree that low priors require more persuasive evidence; our disagreement, therefore, lies 695 mainly in terminology. They imagine discovery-oriented researchers to conduct 696 experiments where they have low expectations that they obtain positive evidence 697 $(.06 \cdot .8 + .94 \cdot .05 = 0.095)$, but if they do, it raises the posterior significantly (from .06 to 698 .51) In our view, researchers who set out to explore a data set often find "something" (due 699 to low $P(\neg E|\neg H)$; therefore, it should only slightly raise your posterior if they do. On a 700 substantive matter, we believe both kinds of research are common in psychology. It is, 701 therefore, mostly a disagreement on terminology. This disagreement only highlights why 702 using a mathematical framework to investigate such things is so useful and ultimately 703 indispensable because we can clearly see where and how we differ in our reasoning. 704

We believe that our reasoning is quite similar to Höfler et al. (2022), who call for 705 transparent exploration using preregistration. We could be more sure of our agreement, if 706 they had formulated their arguments within a mathematical framework, which would also 707 have helped to dissolve an apparent conflict in their definitions of confirmation, exploration, 708 and transparency. On the one hand, they define "The principle difference between 709 confirmation and exploration is that confirmation adheres to an evidential norm for the 710 test of a hypothesis to pass.", but then suggest that transparent exploration can be 711 conducted using inferences tests as a filtering mechanism. Their distinction between 712 confirmation, intransparent and transparent exploration are otherwise just as well placed 713 along the dimensions, theoretical risk and uncertainty about theoretical risk. 714

With the goal to facilitate rigorous exploration, we have proposed a workflow for preregistration called *preregistration as code* (PAC) elsewhere (Peikert et al., 2021). In a PAC, researchers use computer code for the planned analysis as well as a verbal description

of theory and methods for the preregistration. This combination is facilitated by dynamic 718 document generation, where the results of the code, such as numbers, figures, and tables, 719 are inserted automatically into the document. The idea is that the preregistration already 720 contains "mock results" based on simulated or pilot data, which are replaced after the 721 actual study data becomes available. Such an approach dissolves the distinction between 722 the preregistration document and the final scientific report. Instead of separate documents, 723 preregistration, and final report are different versions of the same underlying dynamic 724 document. Deviations from the preregistration can therefore be clearly (and if necessary, 725 automatically) isolated, highlighted, and inspected using version control. Crucially, because 726 the preregistration contains code, it may accommodate many different data patterns, i.e., it 727 may be exploratory. However, while a PAC does not limit the extent of exploration, it is 728 very specific about the probability to generate evidence even when the theory does not hold (theoretical risk). Please note that while PAC is ideally suited to reduce uncertainty 730 about theoretical risk, other more traditional forms of preregistration are also able to 731 advance this goal. 732

Contrary to what is widely assumed about preregistration, a preregistration is not necessarily a seal of confirmatory research. Confirmatory research would almost always be less persuasive without preregistration, but in our view, preregistration primarily communicates the extent of confirmation, i.e., theoretical risk, of a study. Clearly communicating theoretical risk is important because it reduces the uncertainty and hence increases expected persuasiveness.

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744 Declarations

All code and materials required to reproduce this article are available under

https://github.com/aaronpeikert/bayes-prereg (Peikert & Brandmaier, 2023a). The

authors have no competing interests to declare that are relevant to the content of this

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